

# OnFrobenius-EulerPolynomial of high-order convolution formula

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**Abstract:** Study Frobenius-Euler Polynomial Use generation function thought and combination are established. The polynomial of a High-Order convolution formula Makes Dilcher The classic results was as an special obtained.

**Keywords:** Frobenius-Euler Polynomial; Euler Polynomial; Convolution formula

## 1. The introduction and main results

When study power and problem when Switzerl and mathematician Jacob Bernoulli (1654-1705) And Leonhard Euler (1707-1783) Were found there sequence Polynomial  $\{B_N(X)\}_{N=0}^{\infty}$  And  $\{E_N(X)\}_{N=0}^{\infty}$  Can provide beforeNA natural number K Times power and beforeNA natural number of alternating K Times power and of unified formula.<sup>[1-4]</sup> These Polynomial  $B_N(X)$  And  $E_N(X)$  Respectively was called Bernoulli

Polynomial and Euler Polynomial They usually by as follows generation function definition: Special Rational  $B_N=B_N(0)$  And integer  $E_N=2^N E_N(1=2)$  Respectively was called Bernoul li Number of and Euler Number. More Bernoul li Number of and its polynomial and Euler Number of and its polynomial in mathematics of different field in play an important role Which L<sub>1</sub>; In in; L<sub>D</sub>; NA non-negative integer Literature-based [5-7] Okay. Bernoulli Study on the sum formula of the product of numbers, In 1996 Year, Literature [8] Studied (3) Type

Among them

$=X_1 \cdots X_D;$

In view of the above literature research results, This paper will Frobenius-Euler Further research on Polynomial. By applying generative function thought and composition techniques, Establish Frobenius-Euler Polynomial of a High-Order convolution formula. As an application Dilcher Of high-order convolution formula (5) Was as an special situation.

Which DI is a positive integer M; n A non-negative integer And Y = X<sub>1</sub> In in · X<sub>D</sub>. Obvious (8) - In M = 0 The situation that Dilcher Of Formula (5). Similar Theorem 1.1 In M = 0 The situation given. Frobenius-Euler Polynomial

Dilcher High-order convolution formula Its in = -1 The again given Dilcher Of Formula (5).

Which F(X)<sup>(N)</sup> Said F(X) On X Of N-Order Derivative And S(N; d) Is the second class Stirling Number.

$\{F_N(X)\}_{N=0}^{\infty}$  Is a polynomial sequence was to:

$\Sigma_{n=0}^{\infty} F_N(X)^T = F(T) \prod_{k=1}^n (X_k - T),$

N!

N = 0

Here F(T) Is a Power Series.

Syndrome Tomorrow See Literature<sup>[14]</sup>.

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## 4. OfBeam Language

In factWith prove(7)Similar Method of formula,Can also buildBernoulliThe following high-order convolution formulas of Polynomials:

$$(-1)^D \cdot D^{(MN)} \Sigma_{j=1}^D (-1)^{\sum_{k=1}^D (D_k - j)} S_{(D, d_k-j)} Y K_j *$$

Among themDI s a positive integer,M; nNon-negative integer satisfaction  $MN \geq d$ ,And  $Y = X_1 \cdots X_D$ . Apparently, (18)Type

$M=0$ The situation is DilcherFormula(4). (18)Type in  $X_1 = \cdots = X_D = X$  Given Bayad And Komatsu Formula(6) An equivalent form.Literature? [16] Elliptic Type considered in Apodol-Bernoulli Duo

Terms and ellipses Apodol-Euler Polynomial existence and (8)Type and (18)What about the higher-order convolution formula?? In the future, the author will, Further study of the topic.

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